

# Deposition loss of particles in the sampling lines of continuous emission monitoring system (CEMS) in coal-fired power plants

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## Abstract

Facing the severe situation of air pollution, more stringent regulations of pollutant emissions are being promulgated in China, which calls for more accurate and reliable monitoring of particulate matter (PM) emission in coal-fired power plants. In this work we study the sampling loss of CEMS under different conditions by numerically solving particle transport equation in the sampling line. Featuring with a high Reynolds number, the particle deposition loss is severer than conventional laminar sampling and increases with Reynolds number when the plant load changes. The temperature difference between the hot sampling gas and pipe wall has a great effect on the sampling loss of PM 10. A small temperature difference of 2 K, which is very likely to exist even with a thick thermal insulation, will increase the deposition velocity of PM 1-2.5 by ten times. The surface roughness, either from pipe itself or deposited particles, also enhances the deposition loss by partly shifting the capture boundary to a higher diffusivity region. Combined all the possible factors, the loss ratio of 10  $\mu\text{m}$  particles could reach 69% after 0.2 s and 95% after 0.5 s. The loss ratios of 2.5 and 1  $\mu\text{m}$  particles are much lower, but also reach 4.1% and 7.9% respectively after 1 s, which cannot be neglected when a high accuracy monitoring is needed.

**Keywords:** deposition; CEMS; sampling; coal-fired power plant.

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## 34 INTRODUCTION

35

36 Although more stringent regulations of pollutant emissions have been promulgated, the fact of  
37 national-wide haze still indicate a severe air pollution situation in China (Zhang *et al.*, 2012; Gao  
38 *et al.*, 2014; Liu *et al.*, 2014; Zheng *et al.*, 2017; Gao *et al.*, 2017). In 2016, among 338 major  
39 cities, only 84 cities met the air quality standard (Ministry of Environmental Protection of PRC,  
40 2016), which means that the air quality of over 75% cities are still harmful to human health in a  
41 long-term view. The coal-fired power plants of China (Wang *et al.*, 2016; Ma *et al.*, 2017) that  
42 consume more than 50% coal per year, has been recognized as one of the major emission sources.  
43 The upgrade and transformation action plan for coal-fired power energy saving and emission  
44 reduction (2014–2020) which was released in 2014, required the emissions of particulate matter  
45 (PM) of coal-fired power plant to be under 10 mg/Nm<sup>3</sup>(standard situation: 273K, 6% oxygen  
46 content). Though the regulation of PM emission is already quite strict even compared to  
47 developed countries, the accuracy of continuous emission monitoring system (CEMS) and  
48 gravimetric method (often used as the calibration for CEMS) could be the weak point, because  
49 the relative error may become larger for lower emission standard.

50 Installed at the flue-gas stack, the CEMS is mainly composed of a sampling line and a  
51 measuring device. A small portion of flue gas is extracted and measured by some on-line  
52 techniques, for example Beta attenuation or light scattering. Being different from gas phase

53 pollutants, the on-line measurement of PM is always disturbed by deposition loss along the  
54 sampling line. The loss ratio depends on various factors including particle size, flow rate,  
55 temperature difference etc., and sometimes could be quite large. However, the current  
56 specifications for continuous emissions monitoring of flue gas from stationary sources (HJ/T 75-  
57 2017 and HJ/T 76-2017) do not have requirements or guidelines on the sampling loss. Therefore,  
58 a detailed study is needed to address the issue of the sampling loss of CEMS under different  
59 conditions.

60 Compared with Beta attenuation, the light scattering technique has the advantage of  
61 convenience, safety and real-time response, thus widely adopted as the PM monitoring device in  
62 the coal-fired power plant CEMS in China. The typical flue gas velocity in the stack of power  
63 plants is around 20m/s. To keep an isokinetic condition and avoid blockage at the sampling  
64 nozzle, the flow rate of sampling gas is relatively large. Take the STACK-181WS type PM  
65 sensor system of PCME Ltd as an example, the nozzle diameter is 12 mm and the inner diameter  
66 of the sampling pipe is 20 mm. Considering of a sampling velocity of 25 m/s, the Reynolds  
67 number of the sample flow is about 7000, which has fully entered the turbulent regime.  
68 Comparing to conventional aerosol measuring instruments with laminar sampling flows (e.g.  
69 Electrical Low Pressure Impactor (ELPI),  $Re \sim 1000$ ), the highly turbulent flow in CEMS cause  
70 more deposition due to turbulent diffusion for small particles and inertia-eddy impaction for large

71 particles. Moreover, other factors, e.g. the temperature difference between flue gas and  
72 environment, the roughness of sampling pipe surface, could further enhance particle deposition  
73 along the sampling line.

74 The deposition of particles in a turbulent pipe flow is classical. In Lagrangian framework, by  
75 using  $k-\varepsilon$  model, Large Eddy Simulation (LES) and Direct Numerical Simulation (DNS) to  
76 determine the motion of fluid, the motion of particles was computed by Gosman & Ioannides  
77 (1983), Wang & Squires (1996) and Ounis *et al.* (1993). However, the Lagrangian calculations  
78 still face challenges when the number of the particles is important for investigation. For Eulerian  
79 approach, the particle concentration problem can be easily handled by treating particle flow as a  
80 fluid. Based on the remarkable contribution of Friedlander & Johnstone's (1957), the Eulerian  
81 type calculation has been used in engineering solutions for a long time. By considering the  
82 particle inertia and the inhomogeneity of fluid turbulent flow field in an area close to solid  
83 surface, a new mechanism of particle transport which called turbophoresis is proposed by  
84 Caporaloni *et al.* (1975) and Reeks (1983). Guha (1997) established a unified advection-diffusion  
85 Eulerian theory, including molecular and turbulent diffusion, thermophoresis, turbophoresis,  
86 shear-induced lift force, electrical forces, and gravity. Moreover, experimental results on particle  
87 motion in turbulent flow are given by Shimada *et al.* (1993), Lee & Gieseke (1994), El-  
88 Shobokshy (1983), Sehmel (1968) and Liu & Agarwal (1974), among others. The study of

89 particle transport loss in aerosol sampling line mostly focus on the urban environment aerosol  
90 (Birmili *et al.*, 2007; Kumar *et al.*, 2008; Martuzevicius *et al.*, 2008; Kumar *et al.*, 2015). The  
91 particle sampling loss of coal-fired power plant CEMS is more severe than conventional aerosol  
92 measurements due to high Reynolds number of sampling flow, which has not been adequately  
93 studied.

94 In this work we investigate the sampling loss in the CEMS of coal-fired power plants and  
95 discuss various influencing factors. Special attention is paid to the practical conditions of CEMS  
96 to reflect important parameters for different sized particles. The manuscript is organized as  
97 following: Section II describes the numerical method; in Section III, the influences of Reynolds  
98 number, temperature difference and pipe roughness on the particle deposition in the sampling line  
99 are discussed; finally, we make an estimation on the loss ratio of difference sized particles and  
100 the possible underestimation of CEMS.

101

## 102 **METHODS**

103

104 For describing physical process of particle deposition in the Eulerian framework, Guha (Guha,  
105 1997; Guha, 2008) built a unified advection-diffusion theory by assuming particle phase as a  
106 continuous fluid and then deriving this theory from the fundamental Eulerian conservation  
107 equations of mass and momentum for the particles. For fully developed turbulence flow in a pipe,  
108 this theory considered molecular and turbulent diffusion, thermophoresis, turbophoresis, gravity

109 and the drag force. For the boundary condition of the calculation domain, the effects of surface-  
 110 roughness and particle interception are considered. Before we list the equations for this theory,  
 111 note that the particle continuity equation for fully developed flow gives a constant particle mass  
 112 flux in the particle deposition direction, because the particle phase is treated as continuous fluid.

113 For simplicity, the curvature of the sampling pipe is neglected for that the dimension is much  
 114 larger than particle sizes (Guha, 1997). The geometry of the calculation is shown in Fig. 1. The  
 115 particles deposition flux is given by

$$116 \quad J = -(D_B + D_t) \frac{\partial c}{\partial y} - D_T c \frac{\partial \ln T}{\partial y} + c V_{py} \quad (1)$$

117 where

$$118 \quad D_B = \frac{kT(1+2.7Kn)}{3\pi\mu d_p}$$

$$119 \quad D_t = \varepsilon$$

$$120 \quad D_T = D_B(1 + \eta / kT)$$

121 where  $D_B$ ,  $D_t$  and  $D_T$  are the Brownian diffusivity, turbulent diffusivity and the coefficient of  
 122 temperature-gradient-dependent diffusion;  $c$  and  $J$  are the particle concentration and the flux of  
 123 particles;  $y$  and  $V_{py}$  are the perpendicular distance from the wall and the particle mean velocity in  
 124 this direction;  $T$  and  $\eta$  are the fluid temperature and the thermophoretic force coefficient;  $k$ ,  $Kn$ ,  $\mu$   
 125 and  $d_p$  are the Boltzmann constant, Knudsen number, dynamic viscosity and the particle diameter;  
 126 and  $\varepsilon$  is the eddy viscosity of the fluid. The particle deposition velocity  $V_{dep}$ , it is defined as  
 127  $V_{dep} = J/c$ . For the effect of gravitational settling, we have estimated that the terminal settling

128 velocities of 1, 2.5 and 10  $\mu\text{m}$  particles are only 2.1%, 2.6% and 1.9% of the deposition velocities  
 129 respectively under a typical condition in the sampling line. Hence the effect of gravitational  
 130 settling is neglected in this study.

131 Eq. (1) can be numerically solved by combining the particle and the fluid motion equations  
 132 together. The particle velocity can be derived from the particle momentum equations,

$$133 \quad V_{py} \frac{\partial V_{py}}{\partial y} + \frac{V_{py}}{\tau_l} = -\frac{\partial V_{py}^2}{\partial y} \quad (2)$$

$$134 \quad V_{py} \frac{\partial V_{px}}{\partial y} = \frac{1}{\tau_l} (V_{fx} - V_{px}) + (1 - \rho_f / \rho_p) g \quad (3)$$

135 where  $V_{px}$ ,  $V_{py}$  and  $V_{fx}$  are the particle mean velocity in the  $x$  direction, the particle RMS velocity  
 136 and the fluid velocity in the  $x$  direction;  $\rho_f$  and  $\tau_l$  are the fluid density and the inertial relaxation  
 137 time.

138 The fluid motion is described as a function of the wall-coordinate  $y^+$  ( $y^+ = y \times u_* / \nu$ , where  $u_*$  and  $\nu$   
 139 are the fluid slip velocity and the kinematic viscosity). And the functions are summarized in the  
 140 Table 1.

141 To correlate fluid and particle Root Mean Square (RMS) motions, the following correlation is  
 142 adopted (Binder & Hanratty, 1991).

$$143 \quad V_{py}^2 = \Re V_{fy}^2 = [1 + 0.7(\tau_l / T_L)]^{-1} V_{fy}^2 \quad (4)$$

144 where  $T_L = \varepsilon / V_{fy}$  is the Lagrangian time scale. Using the non-dimensional form of  $u_*$ ,  $\nu$ , etc., Eq. (1)

145 and (2) can be normalized as following:

$$146 \quad V_{dep}^+ = -\left(\frac{D_B}{\nu} + \frac{D_t}{\nu}\right) \frac{\partial c^+}{\partial y^+} - D_T^+ c^+ \frac{\partial \ln T}{\partial y^+} + c^+ V_{py}^+ \quad (5)$$

$$147 \quad V_{py}^+ \frac{dV_{py}^+}{dy^+} + \frac{V_{py}^+}{\tau_l^+} = -\frac{d(V_{py}^{+2})}{dy^+} \quad (6)$$

148 where

$$V_{dep}^+ = J / c_0 u_*$$

$$V_{py}^+ = V_{py} / u_*$$

$$c^+ = c / c_0$$

$$V_{fy}^+ = V_{fy}' / u_*$$

$$D_T^+ = D_T / \nu$$

$$\tau^+ = \rho_p^0 d_p^2 u_*^2 / \rho_f 18 \nu^2$$

149  
150 where  $V_{dep}^+$  and  $c_0$  are the non-dimensional deposition rate and particle concentration at the  
151 centerline of the tube.

152 Two kinds of roughness will be considered in this work, the pipe surface roughness and the  
153 deposition roughness (illustrated in Fig. 1). The former one is the inherent rugged surface of the  
154 pipe, and the latter one is caused by deposited particles on the pipe surface. With a similar  
155 method as Grass (Grass, 1971) the starting point of the fluid velocity profile in pipe roughness  
156 cases is chosen as  $0.55k_s$ , where  $k_s$  is the effective roughness height. Under the effect of  
157 interception, the origin of the particle profile is  $0.45k_s + d_p/2$ . For the deposition roughness, we  
158 assume that  $k_s = nl \times d_p$ , where  $nl$  is the number of particle layers.

159

## 160 RESULTS AND DISCUSSION



161

## 162 ***Validation of the method***

163 Fig. 2 shows the comparison between calculation results and different experimental data in  
164 literature. The horizontal axis is non-dimensional particle relaxation, and the vertical axis is non-  
165 dimensional particle deposition velocity. The overall agreement is quite good, considering the  
166 scattered distribution of the literature data. The deviation between the calculation and the  
167 experimental data may due to the surface roughness difference. Three distinct regimes can be  
168 identified by increasing particle relaxation time: turbulent diffusion regime, turbulent diffusion-  
169 eddy impaction regime and particle inertia moderated regime. For practical sampling lines with a  
170 typical Reynolds number of 6000, PM 2.5 ( $\tau^+ \approx 0.58$ , when  $d_p = 2.5 \mu\text{m}$ ) is mainly in the turbulent  
171 diffusion regime and PM 10 ( $\tau^+ \approx 9.2$ , when  $d_p = 10 \mu\text{m}$ ) enters the turbulent diffusion-eddy  
172 impaction.

173 The size range of discharging particles of coal-fired power plants of China is around 0.1~20  
174  $\mu\text{m}$  which locates in the turbulence diffusion and turbulent diffusion-eddy impaction regimes.  
175 Electrostatic precipitator (ESP) is the most widely used major PM removal equipment in China,  
176 and its particle penetration window is 0.1-1  $\mu\text{m}$  (Liu *et al.*, 2016). On the other hand, in order to  
177 meet the ultra-low emission standard of  $\text{SO}_2$ , wet flue gas desulfurization (WFGD) is also  
178 equipped. At the outlet of the WFGD, the concentration of entrained droplet (solid content:  
179 10%~20%) will be mainly reduced by inertial impaction (Zhang *et al.*, 2017) in the demisters.

180 According to the flue gas limestone/limegypsum desulfurization project technical specification  
181 (HJ/T 179 2018) and the datasheet of the commonly used demister (e.g. FLEXICHEVRON style  
182 VIII), the concentration of droplets at the demister outlet is  $50 \text{ mg/m}^3$  with a cutoff diameter of 20  
183  $\mu\text{m}$ . Based on these two facts, we can estimate that the size range of particles in the sampling line  
184 of CEMS is about  $0.1\sim 20 \mu\text{m}$ .

### 185 ***The influence of Reynolds number***

186 Fig. 3 shows the effect of Reynolds number ( $Re$ ) on the deposition velocity of different sized  
187 particles. In practical conditions, the Reynolds number of the sampling flow varies with the  
188 power plant load because an isokinetic condition has to be maintained at the sampling nozzle.  
189 According to a typical sampling velocity of  $10\text{-}30 \text{ m/s}$ , the Reynolds number in the sampling line  
190 (inner diameter  $10\sim 30 \text{ mm}$ ) is within the range of  $5000\sim 15000$  for different monitoring  
191 equipment (e.g. PCME STACK181WS, SDL SCS900PM and SICK FWE200DH). In Fig. 3, the  
192 flow considered are isothermal ( $\Delta T=0\text{K}$ ) and no roughness is assumed at the wall ( $k_s^+=0$  and  
193  $n_l=0$ ), in order to isolate the effect of  $Re$ . The results show that the effect of  $Re$  is quite different  
194 in different regimes. For small particles with short relaxation time, the deposition velocity  
195 increases nearly 3 times when  $Re$  increases from  $6.4\times 10^3$  to  $1.5\times 10^4$ . In this diffusion-controlled  
196 regime, larger  $Re$  leads to larger turbulent diffusivity and thus significantly increases the  
197 deposition velocity. For larger particles entering the diffusion-eddy regime, the effect of Reynolds

198 number becomes much smaller as the contribution of eddy impaction overwhelms turbulent  
199 diffusion. As the particle relaxation time further increases to the inertia-moderated regime, the  
200 effect of Reynolds number again starts to emerge. For instance at a particle relaxation time  $\tau^+$  of  
201 300 (corresponding to a size of larger than 10  $\mu\text{m}$ ), the deposition velocity increases by about  
202 30% as the Reynolds number changes from  $6.4 \times 10^3$  to  $1.5 \times 10^4$ , which shows that the influence of  
203 Reynolds number is less significant compared to the diffusion-controlled regime. The results  
204 indicate that the loss in the sampling line not only changes the total mass of particles but also  
205 changes the size distribution of the sampling aerosol which must be carefully accounted for. The  
206 deviation is larger for larger Reynolds number of sampling flow, especially for PM 2.5. Larger  
207 Reynolds number leads to larger turbulent diffusivity, which significantly increases the sampling  
208 loss of PM 2.5 in the diffusion-controlled regime. In such condition, the size distribution of  
209 CEMS will shift more to large particle size.

#### 210 ***The influence of temperature difference $\Delta T$***

211 Due to the fouling and the corrosion problems, GGH is no longer a common equipment for  
212 coal-fired power plants in China. Therefore, the typical flue temperature of coal-fired power  
213 plants is around 60°C, significantly higher than the environment. Some of the new CEMS use  
214 heated sampling lines to eliminate the influence of the condensation. However, there are still  
215 many CEMS using non-heated sampling lines especially those use dilution sampling method.

216 And it should be noted that the heating of sampling line is not a mandatory term in the latest  
217 specifications yet. In such cases if the thermal insulation is not properly designed, the influence  
218 of thermophoresis will reveal and enhance particle loss in the sampling line. Fig. 4 shows the  
219 effect of temperature difference  $\Delta T$  between the fluid and the wall on the deposition velocity.  
220 From Fig. 4(a), we can see that the influence of thermophoresis is quite remarkable even with a  
221 small temperature difference at the wall. The effect of thermophoresis is most significant to PM  
222 2.5 in the diffusion-controlled regime, and rapidly drops as particle size increases. Fig. 4(b)  
223 shows the dimensionless ratio between particle thermophoretic velocity at  $y^+=0.3$  and deposition  
224 velocity without thermophoresis. The ratio reaches a peak value of about 30 at  $\tau^+=0.2$  for all the  
225 temperature differences, which corresponds to a particle size of about 2  $\mu\text{m}$  at Reynolds number  
226 of 6380. Even for a temperature difference as small as 1 K, the peak value of the ratio can be  
227 larger than 4, showing that thermophoresis largely enhances the deposition loss of PM 2.5 in the  
228 sampling line. We perform a simple heat transfer analysis considering the heat resistances of  
229 forced convection inside the pipe, conduction in the pipe wall and insulation, and natural  
230 convection outside the pipe. The result shows that if assuming the total temperature difference  
231 between the sampling flow and environment is 40 K, the temperature difference between the  
232 sampling flow and pipe wall is about 5 K when the pipe surface is bare and still larger than 3 K  
233 with 10 mm thick thermal insulation. The result suggests that the effect of thermophoresis must

234 be accounted for when evaluating the deposition loss along the piping line even with a thermal  
235 insulation.

236 Moreover, the water vapor in the sampling gas may condense as flowing through the sampling  
237 line if the line is not heated. The condensation on the particle surface could enlarge the size and  
238 thus change the particle dynamics. Here we estimate the possible influence of this effect. With a  
239 heat loss of 9.3 W/m, the mass of total vapor condensation after 2m sampling line is about 7.9  
240 g/Nm<sup>3</sup>. On the other hand, it should be noted that the area of pipe inner surface is over 16000  
241 times larger than the total surface area of air-borne particles, which indicates that most vapor  
242 condenses on the pipe surface. Only a very small fraction of vapor condensation occurs on the  
243 particle surface, which is about 0.47 mg/ Nm<sup>3</sup>. This quantity of condensation only enlarges the  
244 particle size by about 1.6%. Hence, we ignore the effect of vapor condensation on particle  
245 dynamics in this study. For other situations e.g. an even larger heat loss, the effect of vapor  
246 condensation could be significant and needs to be considered.

### 247 ***The influence of roughness***

#### 248 *Pipe roughness*

249 Fig. 5(a) shows the variation of deposition velocity with relaxation time for three different  
250 effective roughness heights. The tendency of the calculation agrees well with the experimental  
251 data in literature. It should be noted that the real roughness of sampling pipe is usually 0~0.5 for

252 plastic pipes and 0.5-1.5 for steel pipes. For PM 10, larger roughness leads to larger deposition  
253 velocity. For even larger particles in the inertia-moderated regime, the effect of surface roughness  
254 is minor. Fig. 5(b) explains the reason why surface roughness enhances particle deposition in the  
255 sampling pipe. The turbulent diffusivity increases with  $y^+$  in the boundary layer. Therefore, with  
256  $k_s^+$  increase from 0.5 to 1.5, the  $D_t/v$  increases by about 10 times, which indicates that the tips of  
257 roughnesses have reached to a region of larger turbulent diffusivity and local particles are more  
258 likely to be captured by these roughnesses. Since turbulent diffusion is an important deposition  
259 mechanism for PM 10 in the sampling line, the effect of surface roughness needs to be considered.

#### 260 *Deposition roughness*

261 Besides natural roughness of pipe inner surface, the accumulation of deposited particles also  
262 produces another type of roughness, here named as ‘deposition roughness’. The critical pull-off  
263 force derived from the Johnson-Kendall-Roberts (JKR) theory is equal to  $1.5\pi wR$ , where  $R$  is the  
264 effective radius between particles and wall, and its value is  $d_p/2$ ;  $w$  is the work of adhesion with  
265 typical values about 10-30mJ/m<sup>2</sup> (Liu et al., 2016). The value of critical pull-off force is about  $10^8$ -  
266  $10^7$  N for micro-sized particles. And the drag force act on the particles located in the viscous  
267 sublayer is about  $10^{-10}$ - $10^{-9}$  N. The comparison between critical pull-off force and drag force  
268 indicates that the re-suspension is not likely to occur in the viscous sublayer and thus the  
269 deposited particles will act in a similar way as natural roughness. In this work, we treat the effect

270 of deposited roughness the same as the pipe roughness, as illustrated in Fig. 1. The enhancement  
271 of deposition velocity due to deposition roughness is shown in Fig. 6. Different from the  
272 influence of pipe roughness, deposited roughness mainly affects the turbulent diffusion-eddy  
273 impaction regime, corresponding to size range 1~10  $\mu\text{m}$ . Similar to the pipe roughness, the  
274 deposition velocity increases with the number of deposited particle layer. If starting from a brand-  
275 new sampling pipe, the accumulation of deposited particles on the inner surface will accelerate  
276 the deposition process, which forms a positive feedback until the deposits grow out of the viscous  
277 sublayer and re-suspend by the flow drag. We can make a rough estimation on the time needed to  
278 form a layer of particles (e.g.  $nl=1$ ). Assuming a particle concentration of  $10 \text{ mg/Nm}^3$  with 44%  
279 PM 10+, the time to reach 50% coverage is less than 7h. The real situation is more complicated  
280 that the deposition roughness of large particles also enhances the deposition of small particles.  
281 Therefore, the effect of deposition roughness needs to be carefully considered.

### 282 ***Underestimation of PM emission due to sampling loss***

283 Based on the above discussions, we can estimate the deposition loss in a sampling line in a  
284 CEMS. The loss ratio  $LR$  is deduced from particle deposition velocity,

$$285 \quad LR = 1 - \exp\left(-4V_{dep}t_r/D\right) \quad (7)$$

286 where  $t_r$  is the residence time of particle in the sampling line, and  $D$  is the inner diameter of the  
287 sampling pipe, taken as 10 mm.

288 Fig. 7(a) shows the loss ratio increasing with the residence time. The dashed lines are the basic  
289 cases at Reynolds number 6380, without considering any temperature difference, pipe roughness  
290 or deposition roughness. The solid lines are the cases of Reynolds number 8680 ( $\Delta Re=2300$ ),  
291 temperature difference  $\Delta T=5$  K, pipe roughness  $k_s^+=1$ , and deposited particle layer  $nl=1$ . As  
292 shown by the dashed lines, the loss ratio of 10  $\mu\text{m}$  particles reaches 60% after a residence time of  
293 1.0 s while the loss ratios of 1 and 2.5  $\mu\text{m}$  particles are both below 0.1%, if no temperature  
294 difference or roughness is considered. With all these effects properly accounted, the solid lines  
295 indicate that the loss ratio of 10  $\mu\text{m}$  particles is nearly 1 and the loss ratios of 1 and 2.5  $\mu\text{m}$   
296 particles increase to 4.1% and 7.9% respectively. Fig 7(b) shows the contribution of each effect.  
297 We can see that for 1 and 2.5  $\mu\text{m}$  particle, the major increases result from the effects of  
298 temperature difference ( $\sim 50$  times) and pipe roughness ( $\sim 25$  times) while the effects of Reynolds  
299 number and deposition roughness are relatively minor. For 10  $\mu\text{m}$  particle, the influences of all  
300 the four factors are close. The results suggest that the sampling loss of large particles ( $\sim 10 \mu\text{m}$ )  
301 must be considered because a major portion of air-borne particles may deposit along the sampling  
302 line and cause a large deviation of CEMS. The loss of PM 2.5 should also be concerned  
303 especially when there is a large temperature difference or surface roughness.

304 Based on the above analysis, we can make a rough estimation on the total amount of PM that is  
305 underestimated due to the sampling loss in CEMS. For simplicity, the size of 1, 2.5 and 10  $\mu\text{m}$  are



306 chosen to represent the loss ratio of PM 2.5, PM 2.5~10, and PM 10+ respectively. Measurements  
307 by ELPI show that the mass fractions (*mf*) of PM 2.5, PM 2.5~10 and PM 10+ are about 42.7%,  
308 13.3% and 44% respectively (Zhao *et al.*, 2016). The total underestimation per standard flue gas  
309 due to sampling loss is given by,

$$310 \quad m_e = ES \times mf_{PM2.5} \times LR_{PM2.5} + ES \times mf_{PM2.5-10} \times LR_{PM2.5-10} + \quad (8)$$
$$ES \times mf_{PM10+} \times LR_{PM10+}$$

311 where *ES* is the emission standard,  $LR_{PM2.5}$ ,  $LR_{PM2.5-10}$  and  $LR_{PM10+}$  are the loss ratio of PM2.5,  
312 PM2.5~10 and PM10+ respectively. We use 10 mg/Nm<sup>3</sup> (ultra-low emission) as the emission  
313 standard, and the residence time is 0.5 s. Calculation results indicate that the underestimation of  
314 the CEMS could be 4.3 mg/Nm<sup>3</sup> with most contribution from PM 10+.

315

## 316 CONCLUSIONS

317

318 In this work we investigate the deposition loss along the sampling line of continuous emission  
319 monitoring system (CEMS) in coal-fired power plants. The deposition velocities of different  
320 sized particles under various conditions are obtained by solving particle transport equation in a  
321 turbulent pipe flow. The loss ratio that could affect the accuracy of CEMS is then calculated for  
322 different conditions. The main conclusions are as following:

323 1) For the typical Reynolds number of sampling flow in CEMS, the main deposition  
324 mechanisms for PM2.5, PM2.5-10, PM10+ are turbulent diffusion, turbulent diffusion-eddy

325 impaction, and inertia impaction. To keep an isokinetic condition at the sampling nozzle, the  
326 Reynolds number in the sampling line may vary in the range of 5000-15000 depending on the  
327 power plant load. Increasing Reynolds number leads to larger deposition velocity in the turbulent  
328 diffusion and inertia moderated regimes but shows little effect in the turbulent diffusion-eddy  
329 impaction regime;

330 2) The contribution of thermophoresis on the deposition loss is quite significant for PM 10.  
331 With a temperature difference as small as 2 K, which is very likely to exist even with a thick  
332 thermal insulation, the deposition velocity of PM 1-2.5 will increase by ten times. This suggests  
333 that in order to obtain an accurate monitoring of PM 10 emission, the temperature of the pipe wall  
334 needs to be equal to or higher than the sampling gas in CEMS;

335 3) The surface roughness, either from pipe itself or deposited particles, will enhance the  
336 deposition loss by partly shifting the capture boundary to a higher diffusivity region. The  
337 influence of pipe roughness is most profound for PM 10 particles, which could be as large as 50  
338 times with a common roughness of 20  $\mu\text{m}$ . This effect needs to be particularly considered for the  
339 start-up stage of CEMS ;

340 4) Combined all the possible factors, the loss ratio of 10  $\mu\text{m}$  particles could reach 69% after 0.2  
341 s residence time and 95% after 0.5 s residence time. The loss ratios of 2.5 and 1  $\mu\text{m}$  particles are

342 much lower, but also reach 4.1% and 7.9% respectively after 1 s residence time, which can not be  
343 neglected if a high accuracy monitoring is expected.

344

## 345 **ACKNOWLEDGMENTS**

346

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350

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438 industrial sources in Yangtze river delta region, China. *Aerosol Air Qual. Res.* 17: 2263–2275.

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440 **Table 1.** Fluid motion functions.

Parameter	Functions
Mean motion of the, fluid in the $x$ direction, $V_{\hat{x}}$	$V_{\hat{x}} = u_* y^+$ <span style="float: right;"><math>y^+ \leq 5</math></span>
	$V_{\hat{x}} = u_* (-1.706 + 1.445 y^+ - 0.04885 y^{+2} + 0.0005813 y^{+3})$ <span style="float: right;"><math>5 &lt; y^+ &lt; 30</math></span>
	$V_{\hat{x}} = u_* (2.5 \ln y^+ + 5.5)$ <span style="float: right;"><math>y^+ &gt; 30</math></span>
Fluid RMS velocity in the $y$ direction, $V'_{\hat{y}}$	$(\overline{V'_{\hat{y}}})^2 = 0.005 y^{+4} u_*^2 / (1 + 0.002923 y^{+2.218})^2$
Temperature profile of the fluid, $T$	$T = \frac{\text{Pr } y^+}{\Delta T_{200}^+} \Delta T + T_w$ <span style="float: right;"><math>y^+ &lt; 5</math></span>
	$T = \frac{5 \text{Pr} + 5 \ln(0.2 \text{Pr } y^+ + 1 - \text{Pr})}{\Delta T_{200}^+} \Delta T + T_w$ <span style="float: right;"><math>5 \leq y^+ \leq 30</math></span>
	$T = \frac{5 \text{Pr} + 5 \ln(1 + 5 \text{Pr}) + 2.5 \ln(y^+ / 30)}{\Delta T_{200}^+} \Delta T + T_w$ <span style="float: right;"><math>30 \leq y^+ \leq 200</math></span>
where Pr is the Prandtl number, $\Delta T$ is the temperature difference between $y^+=200$ and the wall and $T_w$ is the wall temperature.	
Eddy viscosity of the fluid, $\varepsilon$	$\varepsilon = \nu y^{+(4-y^{+0.08})} \left[ \frac{2.5 \times 10^7}{\text{Re}} \right]^{(-y^+ / (400+y^+))} \times 10^{-3}$ where Re is the Reynold number based on the average fluid velocity.

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## Figure Captions

443

444 **Fig. 1.** Illustration of the particle deposition process.

445 **Fig. 2.** Comparison of calculation and experimental data on particle deposition.

446 **Fig. 3.** The dimensionless deposition velocity profile with different Re. ( $k_s^+=0$ ,  $\Delta T=0K$ ,  $nl=0$ )

447 **Fig. 4.** The influence of temperature difference. (a)The dimensionless deposition velocity profile

448 with different  $\Delta T$ ; (b) the  $V_{Tdep}^+ / V_{dep(\Delta T=0K)}^+$  profile. ( $k_s^+=0$ ,  $Re=6.4 \times 10^3$ ,  $nl=0$ )

449 **Fig. 5.** The influence of pipe roughness. (a)The dimensionless deposition velocity profile with

450 different effective roughness height; (b) Variation of the turbulent diffusivity in the y-direction.

451 ( $\Delta T=0$ ,  $Re=6.4 \times 10^3$ ,  $nl=0$ )

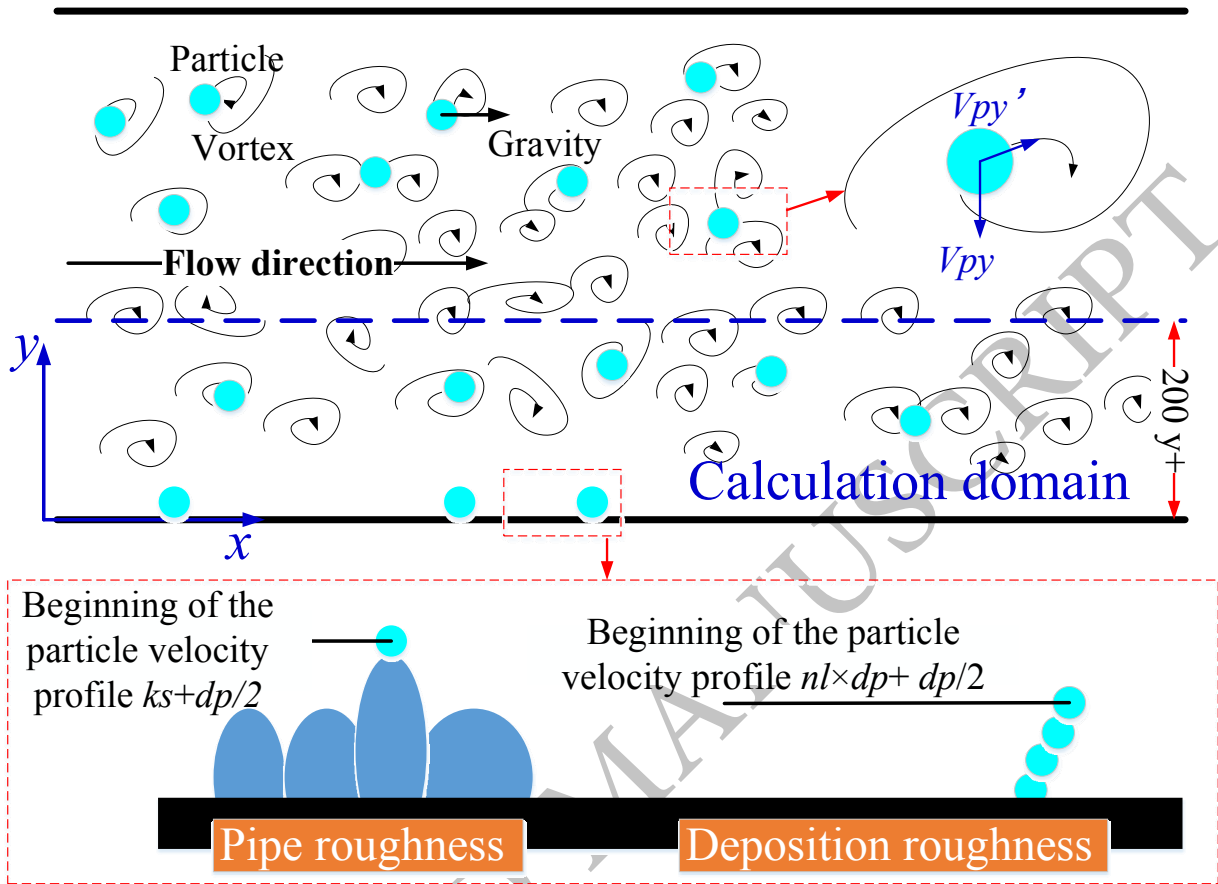
452 **Fig. 6.** The dimensionless deposition velocity profile with different particles layer number ( $\Delta$

453  $T=0K$ ,  $Re=6.4 \times 10^3$ )

454 **Fig. 7.** Variation of the loss ratio for different diameter particles. (a) the particle loss ratio due to

455 increase in residence time. (b) the average loss ratio of different deposition mechanism.

456

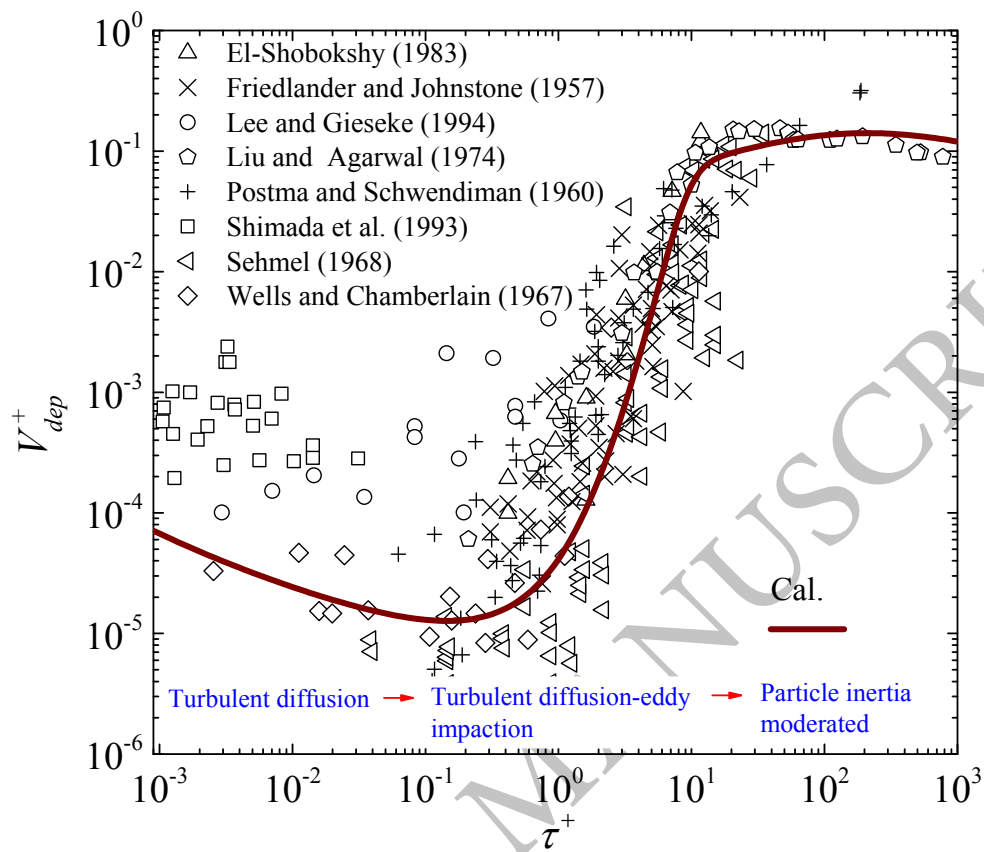


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Fig. 1.



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Fig. 2.

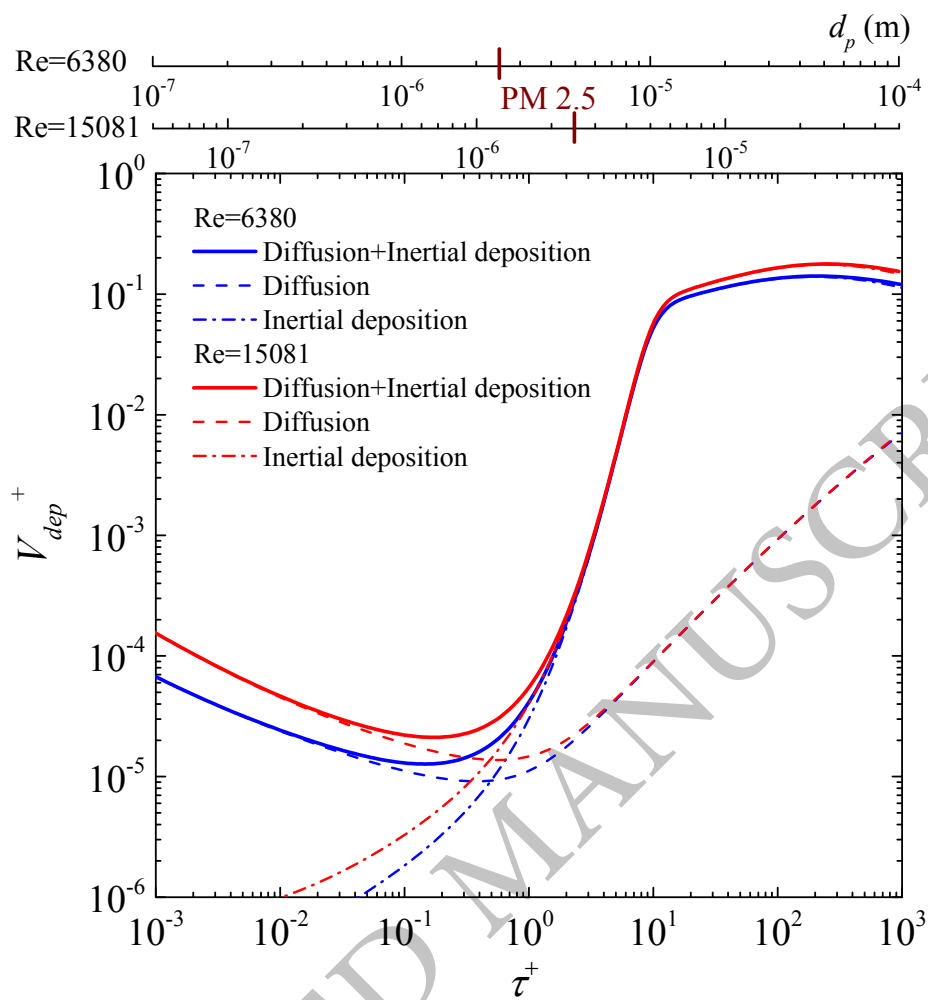
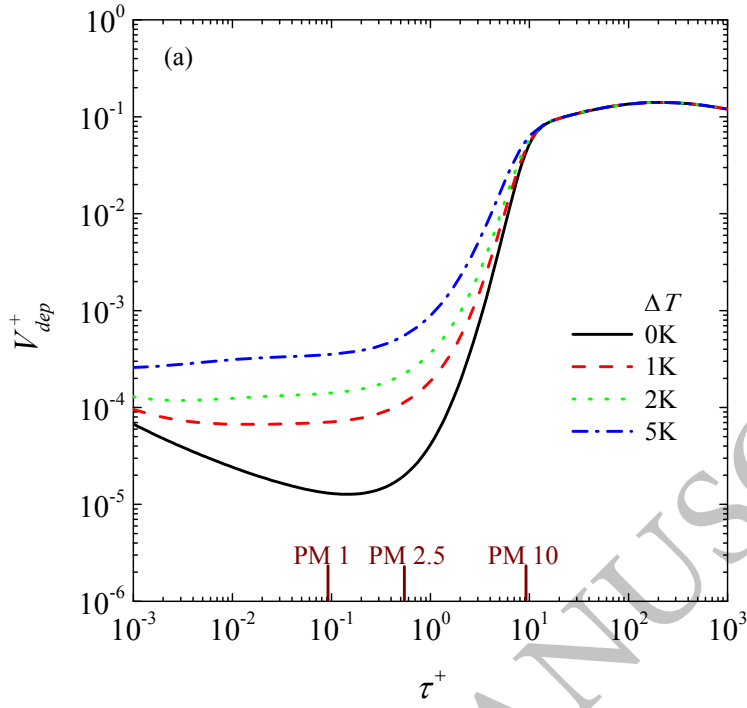


Fig. 3.

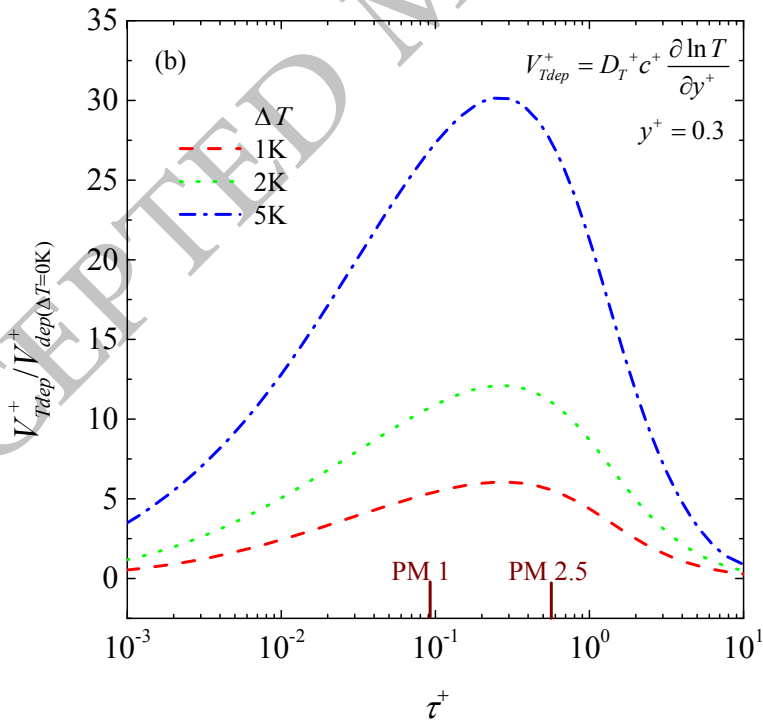
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**Fig. 4.**

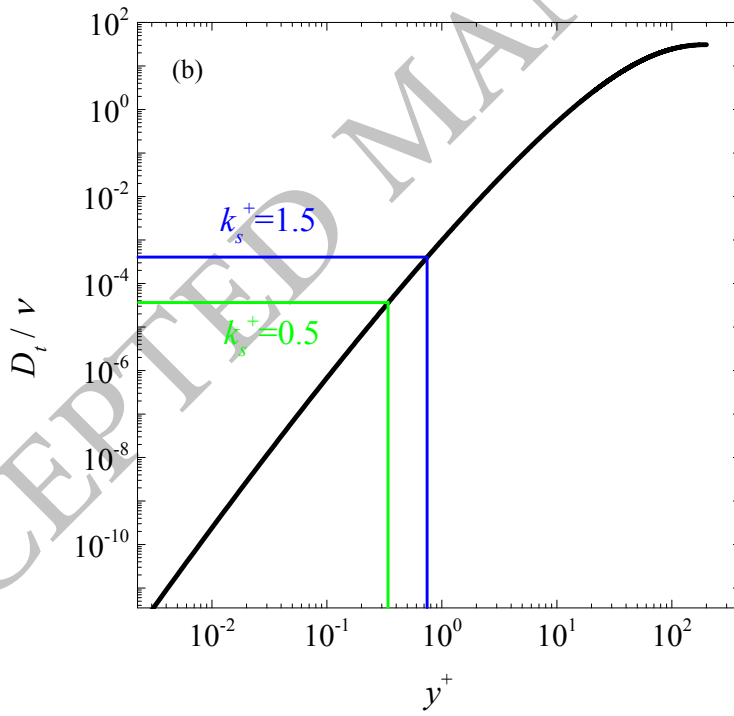
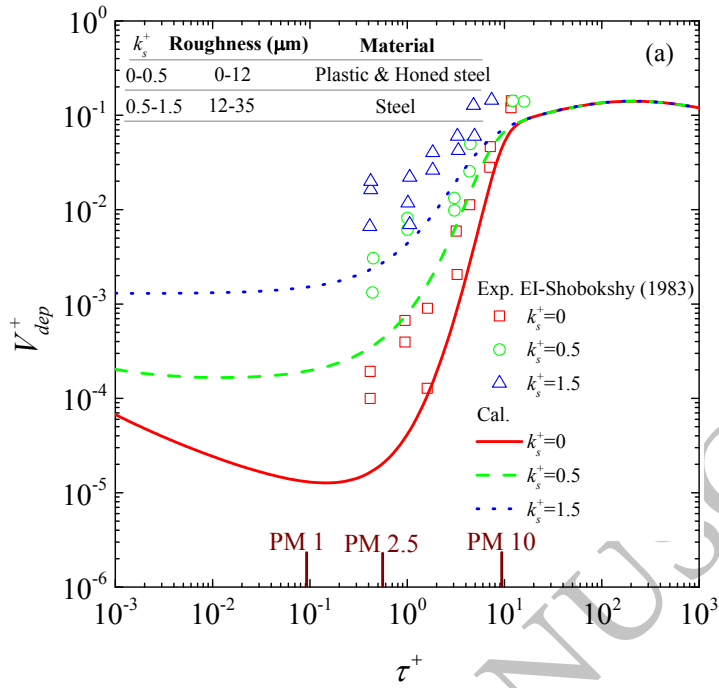


Fig. 5.

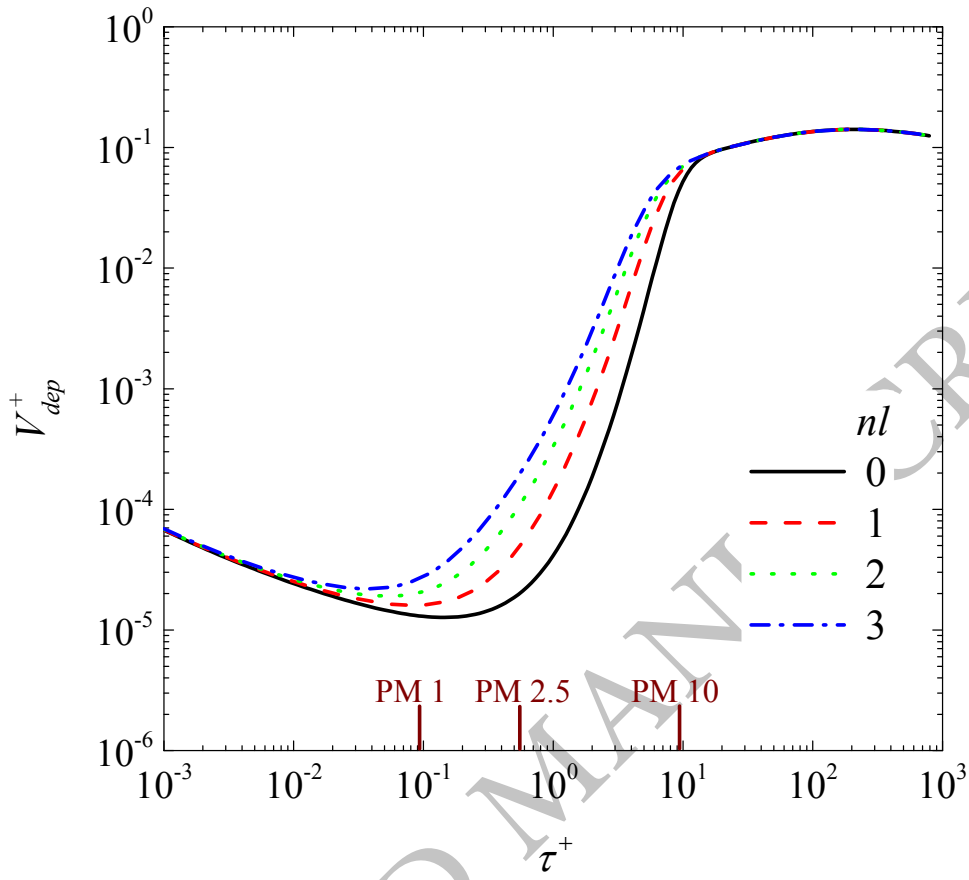


Fig. 6.

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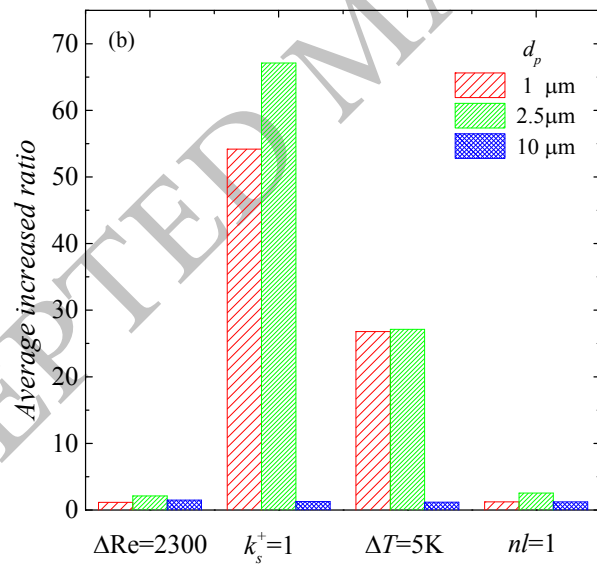
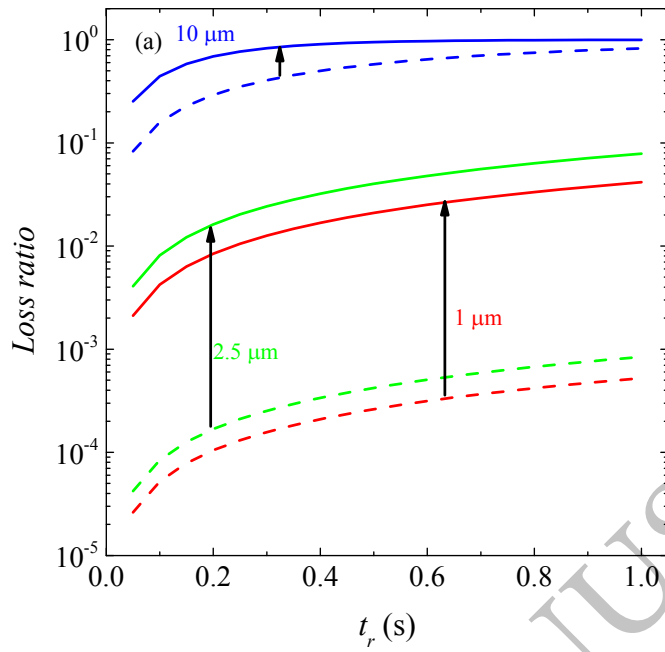


Fig. 7.

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